

Realistic deformable 3D numeric phantom for transcutaneous ultrasound

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Abstract **Introduction:** Numerical phantoms are important tools to design, calibrate and evaluate several methods in various image-processing applications, such as echocardiography and mammography. We present a framework for creating ultrasound numerical deformable phantoms based on Finite Element Method (FEM), Linear Isomorphism and Field II. The proposed method considers that the scatterers map is a property of the tissue; therefore, the scatterers should move according to the tissue strain. **Methods:** First, a volume representing the target tissue is loaded. Second, parameter values, such as Young's Modulus, scatterers density, attenuation and scattering amplitudes are inserted for each different regions of the phantom. Then, other parameters related to the ultrasound equipment, such as ultrasound frequency and number of transducer elements, are also defined in order to perform the ultrasound acquisition using Field II. Third, the size and position of the transducer and the pressures that are applied against the tissue are defined. Subsequently, FEM is executed and deformation is computed. Next, 3D linear isomorphism is performed to displace the scatterers according to the deformation. Finally, Field II is carried out to generate the non-deformed and deformed ultrasound data. **Results:** The framework is evaluated by comparing strain values obtained the numerical simulation and from the physical phantom from CIRS. The mean difference between both phantoms is lesser than 10%. **Conclusion:** The acoustic and deformation outcomes are similar to those obtained using a physical phantom. This framework led to a tool, which is available online and free of charges for educational and research purposes.

Keywords Ultrasound images, Simulation, Numerical phantoms, Elasticity, Linear isomorphism.

Introduction

Diagnostic Ultrasonography (US) has been widely used for more than 50 years and is an established medical imaging technique based on reflected ultrasound waves, which provides tomographic view of subcutaneous structures, important information for diagnosis, therapy and evaluations. However, in some cases, US images alone may not provide sufficient information to objectively and precisely qualify a lesion composition and dangerousness. Therefore, although it has long been used, several researches continuously investigate new image processing tools and methods to improve US diagnostic capability or to create new applications (Ragazzoni et al., 2012), for instance ultrasound elastography and segmentation.

Elastography is an image processing technique in which the mechanical property of tissues is displayed in a strain or elasticity map, which may be produced from images of the target region acquired under different pressures (Céspedes et al., 1993; Dooley, 2012; Kallel and Ophir, 1997; Loree et al., 1994; Ophir et al., 1996). Segmentation consists in delineating or highlighting related objects in an image, providing detailed and objective structural information (Kurnaz et al., 2007).

Physical and Numerical Phantoms are very important tools in many algorithm-development stages of image processing applications (Cardoso et al., 2012; Culjat et al., 2010; Hoskins, 2008; King et al., 2011). Due to the flexibility of controlling parameters and desired features, they are used to calibrate and to evaluate the performance of algorithms; hence, valuable for the development of image systems and techniques, such as filtering (Latifoğlu, 2013), segmentation (Kurnaz et al., 2007) and speckle tracking. In (Culjat et al., 2010) a review on tissue-mimicking physical phantoms for US imaging is described. The physical phantoms may be based on different materials such as condensed milk (Bude and Adler, 1995), agar (Browne et al., 2003) and polyvinyl alcohol cryogel (Liang et al., 2008). Numerical phantoms can be found in (Baldewsing et al., 2004; Bhatti and Sridhar-Keralapura, 2012; Le Floc'h et al., 2009;



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Maurice et al., 2004). Usually COMSOL Multiphysics software (Structural Mechanics Module, version 3.3, COMSOL, France) and ANSYS 5.7[®] software (Ansys, Inc., Cannonsburg, PA) are utilized to compute structural deformations, and MATLAB[®] (MathWorks, Inc., Natick, MA, USA) with Field II (Jensen and Nikolov, 2000; Jensen and Svendsen, 1992) for Ultrasound simulation.

In order to continue improving algorithm performance, creating alternative methods and achieving new breakthroughs, medical images with desirable features are required. Usually, investigators should have access to three sources of images: clinical, physical phantom and numerical phantom. Real US images are not always available for researchers, due to ethics protocols, facilities and difficulties in collaboration policies; and, when they are available, obtaining images with desired features for specific investigation is another difficult obstacle, since parameters and desired features cannot be controlled. Constructing physical phantoms for elasticity purposes may also be a complex task, because selecting corresponding materials to replace the mechanical properties of tissues is difficult (Culjat et al., 2010). In addition, physical phantoms also require US equipment, so that the resulting images can be produced; thus, physical phantoms also require access to facilities or collaborations. Yet, due to computational advancements and techniques, numerical phantoms are becoming more realistic and complete, permitting researchers to execute numerous investigations with controlled and flexible parameters and desired features adjustments (Culjat et al., 2010). Consequently, they are a feasible and practical choice for creating, calibrating and evaluating new methodologies.

Numerical phantoms can be found in prior studies; however, they are not fully covered, as they are not the main topic, but an auxiliary tool for a main investigation. Therefore, approaches fully dedicated to creating of realistically deformable numerical phantoms are important to help investigators to achieve new breakthroughs in US image applications. Consequently, the present approach aims to describe a framework to realistically create deformable numerical phantoms for US applications. In Cardoso et al. (2012), intravascular ultrasound images may be simulated using planar numeric phantom with different intraluminal pressure.

This work presents a detailed framework to produce ultrasound images for transcutaneous applications from a phantom that is able to deform according to the pressure of the transducer surface. In order to simulate the ultrasound acquisition during a procedure with strain in a more realistic fashion, the proposed method consistently displaces the scatterers according to the tissue deformation. This article covers the phantom generation from 3D FEM (Finite Elements Method) to speckle noise simulation. The methodology was embedded in

a Toolbox for MATLAB[®]; the tool is available online at as citationware license type and can be used free of charge for research and educational purposes.

Methods

The proposed framework relies on FEM (Kattan, 2008; Reddy 2006; Zienkiewicz et al., 2010a; 2010b), linear isomorphism (Cardoso et al., 2012) and Field II (Jensen and Nikolov, 2000; Jensen and Svendsen, 1992) to perform realistic deformation, scatterers displacement and transcutaneous ultrasound simulation, respectively, in 3D phantoms. The deformation is performed according to the Young Modulus of each structure, transducer position and applied pressure. The resulting US data is generated by Field II, considering the acoustic parameters of each structure, for instance attenuation and scatterers density.

The material, equipment and software used during development and evaluation of UltraSSim were the elasticity phantom (QA Model 049A from CIRS, Norfolk, VA, USA), ultrasound system (SonixTouch from Ultrasonix, British Columbia, Canada), a personal computer (Intel Core i5, 2.53 GHz, 4 GB of RAM, with Windows 7 64 bits), MATLAB[®] software (MathWorks, Inc., Natick, MA, USA), iso2mesh Toolbox (Fang and Boas, 2009) and Field II (Jensen and Nikolov, 2000; Jensen and Svendsen, 1992).

The evaluation was carried out by calculating the accuracy of structural deformations provided by FEM in the generated phantoms. The resulting strain of the numerical US phantoms were compared with the outcomes from the physical phantom.

The methodology has three main blocks: Numerical modelling, Volume deformation, and US image generation. In Numerical modelling, a 3D volume representing the anatomical subcutaneous features is constructed and loaded (Figure 1a). Subsequently, the different volume structures, corresponding to different tissues of subcutaneous areas, are identified; then, mechanical and acoustic properties are inserted in order to be used by FEM and Field II, respectively. The second section, Volume deformation, uses FEM for the mechanical simulation, where the Young's Modulus for each region, boundary condition, size, position and increment of pressure produced by the transducer are entered. Then, the finite element mesh (χ) is generated using iso2mesh (Fang and Boas 2009) and, with the parameters assigned, the deformed mesh is computed (χ_d) (Figures 1b) (Cardoso et al., 2011; Culjat et al., 2010; Kattan, 2008; Reddy, 2006; Zienkiewicz et al., 2010a; 2010b). Finally, in the US image generation block, the acoustic and strain information provided by the previous blocks is utilized to displace the scatterers through linear isomorphism. Next, Field II is performed to include the speckle noise and

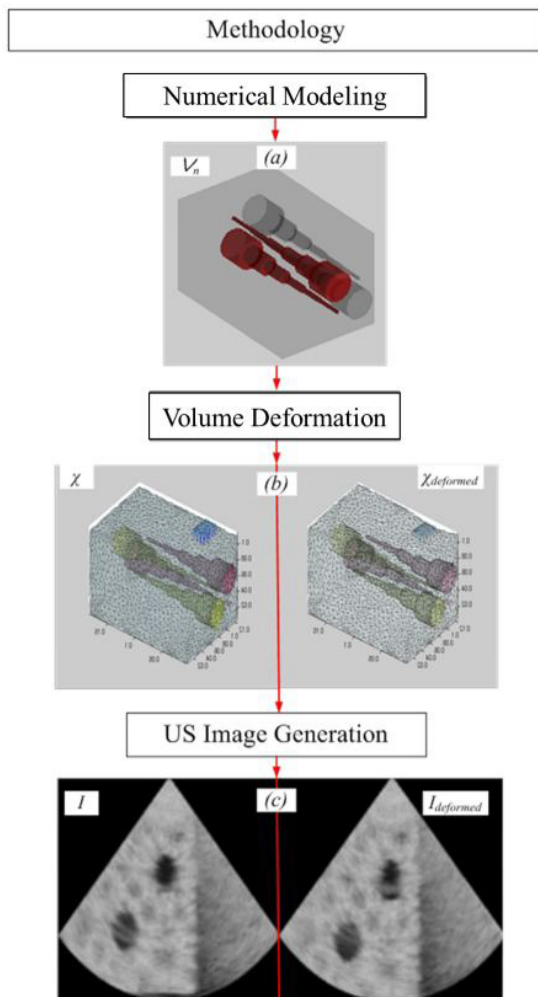


Figure 1. Methodology sequence to obtain the numerically simulated ultrasound images. First, a model representing the target tissue is created. Then, the tissue deformation due the pressure applied by the transducer is simulated through Finite Elements Method and the scatterers are displaced accordingly. Finally, the speckle noise is included using Field II and B-mode images are generated.

generate the noisy non-deformed (I), and noisy deformed (I_{dv}) US images (Figures 1c) (Anton and Rorres, 2005; Cardoso et al., 2011; 2012; Jensen and Nikolov, 2000; Jensen and Svendsen, 1992).

Numerical modelling

As previously described, a transcutaneous US has different applications; hence, the volumetric structure has to be designed to represent the regions of a determined application, for instance cyst, cancer, lipidic, fibrous or calcified tissues, etc. Therefore, the morphological, mechanical and acoustic properties of the volumetric structure must produce US images with corresponding deformation and echoic values in the slice.

The morphology of the volume may be built by combining well-known geometric functions, such as cylinder, spheres and squares, or may be imported from other sources. In this work, the input that governs the morphology of the volumetric phantom was a 3D matrix. In order to distinguish regions, to insert different mechanical and acoustic properties in the different areas, the voxels of each structure is assigned a different value, as illustrated in Figure 2a. If there are two disjoint groups of voxels with the same value, the algorithm should recognize them as being made of the same material. Although we propose creating of volumetric phantoms (3D), a planar view (2D) with low resolution is represented in Figure 2a-c for clarity.

The acoustic and mechanical properties can be regionally inserted by the investigator according to the application. In this work, we created a numerical phantom (Figure 2d), that simulates the physical elasticity QA phantom Model 049A from CIRS (Norfolk, VA, US), which is a physical phantom box that contains a background and isoechoic stepped cylinders representing 4 lesions with different mechanical properties. The Young Modulus of each tissue correspond to $25\pm 6\text{kPa}$, $8\pm 3\text{kPa}$, $14\pm 4\text{kPa}$, $45\pm 8\text{kPa}$, $80\pm 12\text{kPa}$, for the background, and lesions I, II, III, IV, respectively. The phantom width, length and height were 120.0mm, 180.0mm and 95.0mm, respectively. Table 1 summarizes the values of scatterer density and amplitude, attenuation and Young's Modulus of different regions are inserted for each region of the phantom. Although the background and inclusions of the physical phantom are isoechoic, we here considered the inclusions to be hypoechoic in relation to the background. Therefore, it is possible to visualize the inclusions in B-mode images.

In Figure 2d, the transducer surface is represented by a dark blue rectangle. The transducer characteristics are also inserted: features such as position, size and applied pressure, number of active elements at emission and reception, ultrasound center frequency, type of emission - linear or angular direction. In this work, we defined the transducer parameters as shown in Table 2.

Volume deformation

Since we are interested in simulating ultrasound procedures in which theinsonified tissue is under strain, the numeric phantom, along with its structures, must be able do deform realistically. Therefore, in order to perform the simulation of the tissue, a polygonal mesh is generated according to the volume morphology (Figure 3a). Then, the mesh deformation relies on FEM to represent the mechanical features of the volume and its structures, together with the simulation of the dynamics of structural deformation with locally applied pressure (Figure 3b).

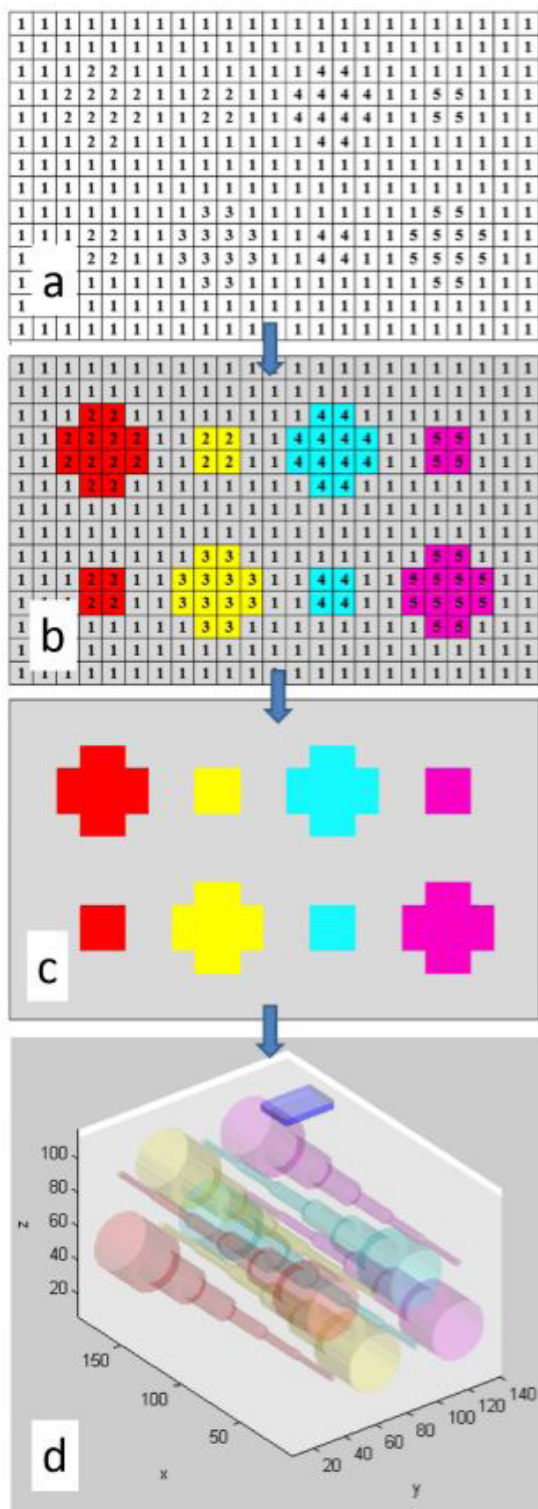


Figure 2. (a-b) Illustration of voxel values to differentiate regions, where each value stands for a different tissue. (b-c) Conversion of the values to color for better visualization. (d) depicts the rendering of the volume that simulates the phantom QA 049A from CIRS, all measures are in mm.

Mesh generation

The mesh is a combination of geometric functions to represent the anatomical and mechanical features of a domain (Kattan, 2008; Reddy, 2006; Zienkiewicz et al., 2010a; 2010b). Since our goal is to investigate the mechanical characteristics of transcutaneous biological tissue using ultrasound image, a mesh corresponding to that structure is created considering the regions and mechanical parameters set previously. Consequently, tetrahedral elements are created (Figure 3a) using the function `iso2mesh` - a free Matlab/Octave-based mesh generation toolbox (Fang and Boas, 2009):

$$\chi = \{ [P_i(\tau), P_j(\tau), P_k(\tau), P_m(\tau), R(\tau)] \mid \tau = 1, \dots, N \} \quad (1)$$

where τ is a tetrahedron element, $P_i(\tau)$, $P_j(\tau)$, $P_k(\tau)$ and $P_m(\tau)$ are the node indices of the corresponding element, $R(\tau)$ is the element homogeneous region, which contains the mechanical properties, and N is the total number of elements of the created mesh.

Strain simulation

The deformation or strain is a shape modification procedure (Figure 3b), related to body stiffness and location, besides strength of applied pressure (Kattan, 2008; Reddy, 2006; Zienkiewicz et al., 2010a; 2010b). The strain simulation uses FEM with the previously inserted mechanical properties to compute the corresponding structural displacements; hence, simulating the deformation caused in the volume according to its stiffness and applied pressure. The elastic properties are stored in the stiffness matrix (K), the computed displacements are put in the displacement vector (U), and the location and value of applied pressure are inserted in the force vector (F) (Kattan, 2008; Reddy, 2006; Zienkiewicz et al., 2010a; 2010b). In this study, we utilized Poisson's ratio $\nu = 0.495$; hence, the material is considered to be nearly incompressible, isotropic and homogeneous (Korte et al., 1999; Le Floc'h et al., 2009).

Force vector F is represented by the resulting vector force obtained by the applied pressure, area and location of the transducer. Therefore, the probe force vectors f_{probe} are obtained by the applied localized pressure P from the transducer, and its area A_{probe} (Figure 4). Consequently, the nodes corresponding to the face where the pressure is applied receives the computed probe force vectors f_{probe} :

$$F(node) = \frac{f_{probe} \times A_{\Sigma face}}{A_{probe}} \quad (2)$$

in which $F(node)$ is the force at the node (Figure 4), A_{probe} is the area of the surface of the transducer in contact with the tissue and $A_{\Sigma face}$ is the sum of the areas of the faces to which the node belongs and are in the interface tissue/transducer.

Table 1. Parameters used to simulate the phantom QA 049A from CIRS.

Parameter	Background	Type I (red)	Type II (yellow)	Type III (blue)	Type IV (pink)
Young Modulus (kPa)	25	8	14	45	80
Scattering Amplitude	5	1	1	1	1
Scatterers Density (units/mm ³)	3	3	3	3	3
Attenuation (dB/MHz/cm)	0	0	0	0	0
Diameter of the insonified Cylinder (mm)	-	10.4	10.4	10.4	10.4
Distance between insonified cylinder and phantom surface (mm)	-	30	30	30	30

Table 2. Transducer specifications used during deformation and ultrasound simulation.

Parameter	Unit	Value
Number of applied forces (frames)		2
Applied Forces	kgf	0 and 1.5
Phantom Resolution	μm/Voxel	1000
Transducer Width	mm	30
Transducer Height	mm	20
Number of elements		64
Number of Active Elements during Emission		1
Number of Active Elements during Reception		16
Element Width	μm	440
Element Height	μm	5000
Distance Between adjacent Elements	μm	50
Distance Between Elements and Tissue	mm	3
Number of Emitted Ultrasound beams		75
Ultrasound Center Frequency	MHz	3.5
Ultrasound Sampling Frequency	MHz	100
Ultrasound Speed	m/s	1540
Geometric Focus	mm	64
Depth of ROI	mm	90
Type of emission – linear or angular		angular

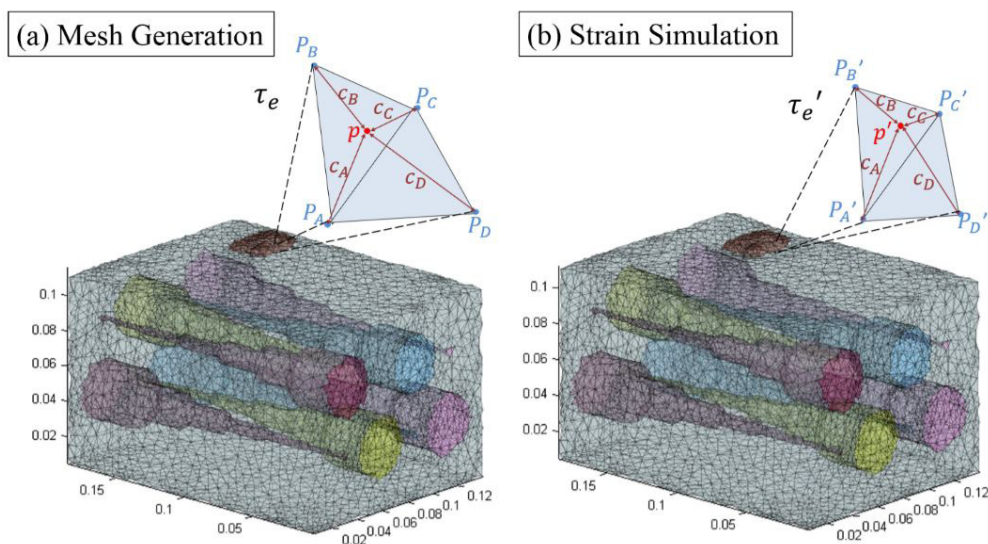


Figure 3. Volume Deformation Blocks. (a) Mesh generated with the illustration of the scatterer position p inside a magnified tetrahedral element before compression. (b) Strain Simulation after the locally applied pressure and scatterer reallocation according to the tetrahedron deformation using linear isomorphism.

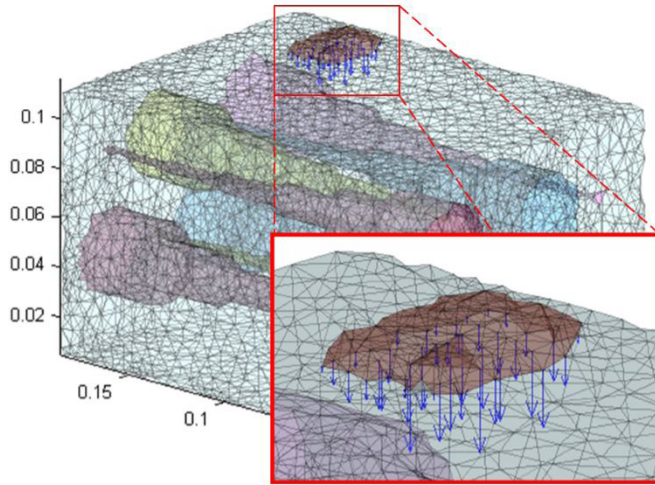


Figure 4. Close look at the transducer location. The blue arrows depict the force applied at the nodes located in the interface between the tissue and the transducer.

We considered that the box that encloses the phantom is non-deformable. Therefore, the opposite and lateral walls, in relation to the applied pressure location, are assigned as boundary conditions and they do not move during deformation.

US image generation

Realistic US Images are created from the localized volume slices by adapting Field II to the application. Field II is a program that utilizes the concept of spatial impulse responses for simulating ultrasound transducer fields and ultrasound imaging using linear acoustics (Jensen and Nikolov, 2000; Jensen and Svendsen, 1992). In order to accomplish that, the US image Generation contains four steps: Scatterers distribution, Linear isomorphism, RF simulation, and B-mode ultrasound image construction (Culjat et al., 2010).

Scatterers distribution

The scatterers are uniformly distributed inside each volumetric FEM element according to the regional acoustic parameters inserted during the Numerical Modelling section. Therefore, first, the number of scatterers of each element is calculated as follows:

$$N_{elem} = V_{elem} \cdot D_R \tag{3}$$

where V_{elem} is the element volume and D_R is the scatterers density of a region, to which the element belongs. Second, N_{elem} are uniformly distributed inside the elements with the corresponding intensities, generating a matrix of scatterer intensities and disposition inside

the volume (I^{scat}), this matrix will be used to generate the non-deformed US image (I) (Figure 1c).

Linear isomorphism

Due to the deformation, the set of scatterers (I^{scat}) must have their initial location modified according to the structural displacement, generating the matrix of scatterers post deformation (I_d^{scat}). Therefore, in order to reproduce real image acquisitions, pre and post-deformation, morphism procedure is carried out (Figure 3).

In order to compute the corresponding matrix of scatterers for the deformed volume (I_d^{scat}), we first associate each scatterer position from I^{scat} to the element it belongs to, by computing the coordinates of the scatterer in relation to the node positions $\{PA, PB, PC, PD\}$ of its element τ . Therefore, each scatterer will have a position $p = \{x, y, z\}$, determined by four constants relative to the element $\{c_A, c_B, c_C, c_D\}$ (Figure 3a); hence, p is defined as:

$$\begin{aligned} x &= c_A \cdot x_A + c_B \cdot x_B + c_C \cdot x_C + c_D \cdot x_D \\ p &= c_A \cdot P_A + c_B \cdot P_B + c_C \cdot P_C + c_D \cdot P_D \rightarrow y = c_A \cdot y_A + c_B \cdot y_B + c_C \cdot y_C + c_D \cdot y_D \tag{4} \\ z &= c_A \cdot z_A + c_B \cdot z_B + c_C \cdot z_C + c_D \cdot z_D \end{aligned}$$

In order to ensure that the scatterer is inside the tetrahedral element, the following rules must be satisfied:

$$0 \leq c_A, c_B, c_C, c_D \leq 1 \tag{5}$$

and

$$c_A + c_B + c_C + c_D = 1 \tag{6}$$

Once the tetrahedron element is deformed, the element nodes are moved to new positions $\{P'_a, P'_b, P'_c, P'_d\}$; hence, the scatterer position will also be reallocated $p' = \{x', y', z'\}$ (Figure 3b). Assuming that the transformation is linear, the constants $\{c_A, c_B, c_C, c_D\}$ will be the same after deformation. Consequently, the new scatterer position p' can be computed by knowing the new node positions after FEM deformation $\{P'_a, P'_b, P'_c, P'_d\}$; thus (Figure 3b):

$$p' = c_A \cdot P'_a + c_B \cdot P'_b + c_C \cdot P'_c + c_D \cdot P'_d \rightarrow \begin{cases} x' = c_A \cdot x'_A + c_B \cdot x'_B + c_C \cdot x'_C + c_D \cdot x'_D \\ y' = c_A \cdot y'_A + c_B \cdot y'_B + c_C \cdot y'_C + c_D \cdot y'_D \\ z' = c_A \cdot z'_A + c_B \cdot z'_B + c_C \cdot z'_C + c_D \cdot z'_D \end{cases} \quad (7)$$

By performing the morphism, the corresponding slices of the final US phantoms (Figure 1c), will reproduce realistic speckle aspects, including the dynamic of tissue movement.

RF simulation

The RF simulation is performed using Field II developed by (Jensen and Nikolov, 2000; Jensen and Svendsen, 1992). Specifically, the transducer characteristics introduced at the numerical modelling section are recalled with a sampling frequency preset to 100MHz to perform the ultrasound beamforming. Then, it considers the set of scatterers, I^{scat} , to calculate the received signal S . Analogously, the procedure is repeated for the case with

deformation and I^{scat} is utilized to obtain S_d . In order to reduce computation time, the corresponding RF signal from the I^{scat} and I_d^{scat} are generated taking into consideration only the scatterers located within a slice of the phantom with 15 mm-thickness.

B-mode ultrasound image generation

The B-mode images (Figure 5) are created by first computing the envelope of S , generating S_{env} :

$$S_{env} = |S + i * H(S)| \quad (8)$$

in which H is the Hilbert Transform and i is the imaginary unit.

The intensity of the signals related to the highly echogenic regions hinders the visualization of hypoechoic structures. Therefore, in order to reduce the dynamic range of the received signals for efficient display, compression is performed by a log function:

$$S_{log} = \log(S_{env}) \quad (9)$$

Next, since the RF resolution is higher than the B-Mode the resulting signal is down sampled with the following sampling factor:

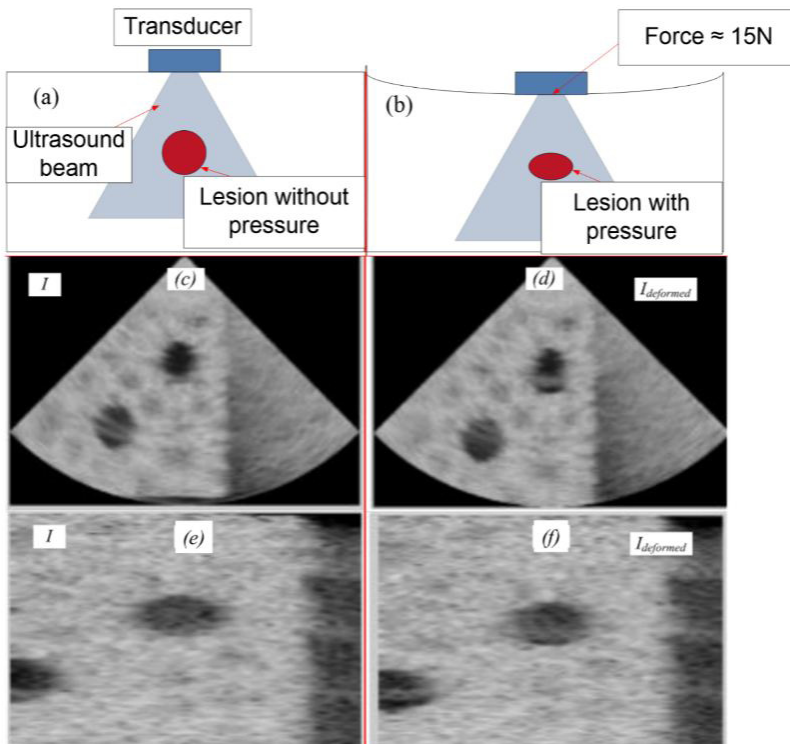


Figure 5. B-Mode Ultrasound Image Generation. (a) and (b) illustrate how the image acquisition of the physical phantom was performed without and with pressure, respectively. The final noisy images constructed with RF generated with angular (c and d) and linear (e and f) emissions for the non-deformed I (c and e), and deformed $I_{deformed}$ (d and f) volume slice.

$$D = \frac{Res_{US} * f_s}{c} \quad (10)$$

where f_s is the sampling frequency preset to 100MHz, Res_{US} is the desired US image resolution and c is the US speed. Finally, the resulting lines are distributed linearly or angularly, according to their position during acquisition, and a bilinear interpolation finishes the B-mode construction (Figure 5).

Results

The evaluation focuses on the FEM deformation accuracy, as the US images are generated by Field II, a widely used method for US image generation and corroborated in other occasions (Cardoso et al., 2012; Jensen and Nikolov, 2000; Jensen and Svendsen, 1992). Therefore, the rating was carried out by comparing the deformation obtained from the numerical phantoms created with the results from the physical phantom (CIRS Elasticity QA Phantom, Model 049 A). In order to accomplish this task, first, US images from the different “lesions” of the physical phantom were acquired without pressure and with a specific pressure. Next, a numerical volume representation of the Phantom QA Model 049A was created, and phantom images generated in the same conditions as the real acquisition. Finally, the resulting strains of the lesions investigated from the numerical and physical phantoms were compared and the correspondence between them was corroborated.

US images acquisition from physical phantom

The US data acquisitions of the physical phantom were performed using ultrasound system with the transducer (4-2MHz) (SA4-2/24). The target lesions had 10.4 mm diameter and the center was located 30 mm below the phantom surface. For each lesion of the physical phantom, 10 Cross section images were acquired independently without (Figure 5a) and with pressure (Figure 5b). The force applied was approximately 15N, obtained by pressing the transducer with 1.5kg. Although this force is greater than the force used in clinical practice, it was used here to facilitate the visualization of the compression. This value was chosen taking into consideration a good trade-off between producing an identifiable strain ratio and not damaging the phantom. The transducer surface measures approximately 3cm x 2cm.

By having the RF maps, the lesions were manually segmented and the diameter was measured in the same direction as the transducer axial direction in both uncompressed and compressed images. Then, the linear strain ratios of the lesions were computed as follows:

$$\varepsilon = \frac{L - L_0}{L_0} \quad (11)$$

where L_0 and L are the lesion diameter before and after compression, respectively.

The obtained linear strain values are shown in Table 3.

Numerical phantom creation

A numerical volume representing the Phantom QA Model 049A was created (Figure 2d). The locations, dimensions and features of the box and lesions are the same as the physical phantom QA Model 049A datasheet (CIRS..., 2013). The numeric phantom properties are shown in Table 1.

The FEM deformation was performed with the same transducer dimension, locations, and applied force as the real acquisition. The boundary conditions were considered setting static the nodes located at the bottom and lateral wall of the box.

The ultrasound simulation was performed using Field II. The excitation was a two-cycle sine function and the impulse response for both emission and reception was a Hanning weighted two-cycle sine function. All parameters and values are summarized in Table 2.

A displacement map was generated using the information from the FEM deformation, and then the linear strain was calculated as follows.

$$\varepsilon = \frac{\delta(p_U) - \delta(p_L)}{p_U - p_L} \quad (12)$$

where p_U and p_L are the lesion upper and lowest pixel position and $\delta(p_U)$ is the displacement of pixel p .

The calculated linear strains of the numeric phantom are shown in Table 3.

The computational time used to perform the numerical modeling was 1.93±0.24s, while the FEM deformation consumed 114.91±13.74s and the linear deformation took 14.36±2.27s to be completed. The RF simulation provided by Field II had an average of 33.82±1.25s per ultrasound signal.

Table 3. Strain values (%) produced by the Physical and Numerical Phantoms.

Phantom	Lesions strain (%)			
	Type I 8±3kPa	Type II 14±4kPa	Type III 45±8kPa	Type IV 80±12kPa
Physical	10.1±2.1	9.81±1.39	4.88±1.77	3.84±0.65
Numerical	11.0±3.2	8.86±1.48	5.69±0.81	3.60±0.71

The results were obtained from a set of 10 simulations with different scatterers distribution.

As can be observed, the strain values produced by the numerical and physical phantoms are very similar. In addition, by running the t student test, the null hypothesis is not rejected with significance level $\alpha=0.001$, corroborating the mechanical similarity between the two phantoms.

Discussion

A framework devoted to realistic transcutaneous phantoms was described. To our knowledge, no previous work involving numeric 3D phantom deformation, scatterers displacement and speckle noise simulation in only one platform has been published. Baldewsing et al. (2004) and Le Floc'h et al. (2009) used FEM to simulate a 2D model to predict arterial strain behavior. In Bhatti and Sridhar-Keralapura (2012) a 3D software breast phantom was built using a mechanical design tool, to investigate the biomechanics of elastography using FEM. Although the authors designed the phantom to be flexible in both, the breast geometry and biomechanical parameters, there was no further ultrasound simulation. In Maurice et al. (2004), FEM was used to calculate the strain and included the speckle noise in the images considering the acoustic impedance of each structure, with no regards to the consistency of the scatterers displacement.

Differently from the other techniques presented in the literature, we developed a method that consistently displaces the scatterers according to the results from the FEM. In other words, we consider that the scatterers map is a property of the imaged tissue that should move according to the tissue strain. The proposed approach was embedded in a Matlab Toolbox as a citationware. It may be used freely for research and educational purposes, and is found online at IVUSSim website (Universidade..., 2012). The methodology is divided into three parts: Numerical modelling, Volume deformation, US image generation. The first informs how a volume representing anatomical features may be constructed. In the second, FEM is used for the mechanical simulations of structures. Finally, in the third block, Field II and linear isomorphism are again combined (Cardoso et al., 2011; 2012) to create realistic pre-compression and post-compression US images. Future works may include different beamforming strategies, such as plane wave compounding and Fourier imaging.

The phantom visual results (Figure 5) with the deformation values corroborated with physical phantom under real acquisitions demonstrate the reliability and usefulness of the framework. Among the combination of methods to produce a unique transcutaneous phantom

based on 3D deformable volumes, the major contributions of this framework is a 3D morphism procedure, in which a 3D FEM mesh is connected to the scatterers providing a novel routine of a real 3D scatterer reallocation. Consequently, realistically scatterers shifting due to regional deformation are reproduced by the generated phantoms. Since Field II (Jensen and Nikolov, 2000; Jensen and Svendsen, 1992) is a widely used and established technique, the evaluation focused on the 3D FEM accuracy, corroborated by comparing the strain results (Table 3) from numerical and physical phantoms under the same condition and similar parameters. Additionally, the student t test demonstrated that the null hypotheses of both strain results, numerical and physical, is not rejected with confidence above 99.9% for all tissues.

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Erratum

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Where it reads:

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